# Genetic Algorithm Approach to reconfigure alternatives in the Supply Chain Network

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Supply Chain Management (SCM) has been drawing much attention for most companies. Among others, the reconfiguration of the existing Supply Chain Network (SCN) is essential to retain their competitive edges. In the strategic level, however, even if we focus on the quantitative criterion such as cost, however, there are situations that it is not easy to aggregate various costs into the overall cost, because of their imprecision, indetermination and uncertainty. Furthermore, other qualitative criteria must be taken in to account for evaluating the performance of supply chain network. In these complex situations, the heuristic analysis which has been frequently used is the best suited.

This paper presents a genetic algorithm method. It has been implemented in the evaluation of several reconfiguration alternatives of the warehouses distributed all over the nation, especially focusing on the warehouse in North East region in Japan, of a major household appliances company. Furthermore, we suggest a new coding method which using matrix form to control the lethal gene in network problem.

Keywords: supply chain network, genetic algorithm, multicriteria analysis, lethal gene

## 1. Introduction

In the 1980s companies discovered new manufacturing technologies and strategies that allowed them to reduce costs and better compete in different markets. Strategies such as just-in-time manufacturing, kanban, lean manufacturing, total quality management, and others became very popular, and vast quantities of resources were invested in implementing these strategies. In the last few years, however, it has become clear that many companies have reduced manufacturing costs as much as is practically possible. Many of these companies are discovering that effective supply chain management (SCM) is the next step they need to take in order to increase profit and market share.

Nowadays, the importance of SCM has been recognized worldwide, and many companies have been applying this concept. From the production to the delivery of the products to the consumers; retailers, wholesalers, manufacturers and material supplier are closely related and form a chain called the 'Supply Chain'. Initially the efficiency of distribution system has been dealt only by an individual company. However, eventually, all the companies related to a specific product started adopting SCM to minimize the system wide costs while satisfying service level requirements.

One of the most advanced cases in SCM is the "direct" model, which gives Dell computer direct

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access to their final customers, by making use of information technology and unifying the production, distribution, and sales information. Further, cross-docking system employed by Wal-Mart, continuous replenishment program (CRP) developed by P&G, efficient consumer response (ECR) in the grocery industry and quick response (QR) in fiber-related industries have been successfully implemented.

There are various SCM issues. One is the network configuration decision regarding the number, location, and capacity of warehouses and manufacturing plants. So far, mixed integer programming models have been widely used to configure facility locations, and improve overall operations (See, for instance, Shapiro[9]).

The reconfiguration of the existing supply chain network is essential to retain their competitive edges. In the strategic level, however, even if we focus on the quantitative criterion such as cost, it is not unusual that various costs involved in supply chain network cannot easily be aggregated into the overall cost, because of their imprecision, indetermination and uncertainty. Furthermore, there are other qualitative criteria to evaluate the performance of supply chain network. In these complex situations, as an overall evaluation, for instance, a simple weighted sum of criteria is not adequate. Instead, the outranking analysis which has been frequently used is the best suited. So far, various variants of the meta-heuristic algorithms, which are called Genetic Algorithm, Simulated Annealing, Tabu Search and others. These have, however, a weakness because of their arbitrariness at the same time and difficulty of coding.

We present a Genetic Algorithm to decide an optimal a number of warehouses with a new coding method. As an illustrative application, we adopted a Shapiro's data [9] to evaluae various reconfiguration alternatives of the warehouses distributed all over region.

## 2. Genetic Algorithm: GA

The Genetic Algorithm (GA) is an adaptive heuristic search method based on population genetics. The basic concepts are developed by Holland (1975) [7], while the practically using the GA to solve complex problems is demonstrated in Dejong (1975) [2] and Goldberg (1989) [4]. References and details about genetic algorithms can also be found for example in Alander (2000) [8] and Mülenbein (1997) [6] respectively.

The creation of new generation of individuals involves primarily four major steps or phases: representation, selection, recombination (crossover), and mutation. The representation of the solution space consists of encoding significant features of a solution as a chromosome, defining an individual member of a population. Typically pictured by a bit string, a chromosome is made up of a sequence of genes, which capture the basic characteristics of a solution. The recombination or reproduction process makes use of genes of selected parents to produce offspring that will form the next generation. It combines characteristics of chromosomes to potentially create offspring with better fitness. As for mutation, it consists of randomly modifying gene(s) of a single individual at a time to further explore the solution space and ensure, or preserve, genetic diversity. The occurrence of mutation is generally associated with low probability. A new population replaces those from the old one. A proper balance between genetic quality and diversity is therefore required within the population in order to support

efficient search.

Although theoretical results that characterize the behaviour of the GA have been obtained for bitstring chromosomes, not all problems lend themselves easily to this representation. This is the case, in particular, for sequencing problems, like vehicle routing problems, where an integer representation is more often appropriate. We are aware of only one approach by Thangiah (1995) [11] that uses bit string representation in vehicle routing contexts.

A basic scheme of a typical algorithm is as follows.

Randomly create an initial population

While not (termination condition)

do

Evaluate each member's fitness

Kill the bottom x% elements of the population

Let the fitness reproduce themselves

Randomly select two members/parents (many other selection

methods are also used)

Perform crossover on the selected elements to generate two children (many variations

of crossover exist)

Perform mutation

#### **Endwhile**

## 3. A Case Study: Reconfiguration Problem of Company A

Company A has many warehouses and agents all over Japan. There is a long demand chain of A's products consisting of construction dealers, agents, business offices, enterprises, and plants/ factories. The distribution process of company A is illustrated in Figure 1. As shown in Figure 1, the logistics network of A comprises of on one-stage distribution system, where the warehouses are supplied from a factory. In order to secure one-day delivery service, warehouses are distributed in local regions. Since, there are many restrictions (capacity of warehouses, variety of demand, etc.), it is a difficult and impractical process to store all items in the warehouses. Moreover, Company A has a problem, how many warehouses are needed.

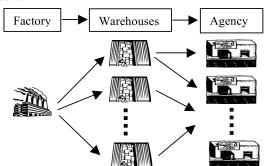


Figure 1. Company A's distribution process

### **Problem Formulation**

We are examining the effectiveness of merging some warehouses distributed all over the nation. Some of the advantages of merging are as follows:

- (a) to reduce the safety inventory.
- (b) to reduce the operating cost.

#### Cost

It is difficult to aggregate distribution, handling and storage cost, into an overall cost, because it is difficult to estimate precisely cost values due to time and cost constraints. Therefore, we have decided to look at all these costs separately.

## **Total inventory**

Estimate the warehouses stock/inventory.

Since lesser the inventory stock, the better, this is a minimization criterion.

#### Restrictions

Consider capacities of warehouses and agencies

Each agency can receive the products from just one warehouse

#### **Numerical Study**

Our numerical experiments were run on a MacBook Intel Core Duo-2GHz Processor, MacOsX Operating System using the Program Language C. We tested two methods; Genetic Algorithm and Branch and Bound method, so as to evaluate the performance using a data of Shapiro[9]. We found that the speed of convergency is very sensitive to the setting of GA-parameters. However, the computational study on set of benchmark problems indicated that our GA-based heuristic is capable of generating optimal solutions for small-size problems as well as high-quality solutions for large-size problems. The algorithm outperforms any of the previous heuristics in terms of solution quality. The computational times of the algorithm are very reasonable for all problem instances from the heuristic viewpoint. In addition, the numerical experiment used a delivery plan problem, which is shown as below Table 1.

|   | fixed cost |        | a        | b        | c        | d        | e        | f       | g        | h       |
|---|------------|--------|----------|----------|----------|----------|----------|---------|----------|---------|
| Α | 134        | A      | 148.5828 | 169.287  | 113.022  | 130.4688 | 256.128  | 112.29  | 63.6528  | 25.05   |
| В | 140        | В      | 156.6288 | 154.9092 | 72.8364  | 53.7972  | 103.2516 | 13.002  | 29.904   | 207.414 |
| С | 160        | С      | 197.3952 | 176.7078 | 79.2948  | 38.124   | 22.4112  | 73.284  | 22.8552  | 324.648 |
| D | 225        | D      | 389.4264 | 349.2414 | 213.486  | 196.1268 | 275.3376 | 261.222 | 62.7984  | 576.15  |
| E | 142        | E      | 284.292  | 273.1782 | 165.7656 | 152.496  | 212.9064 | 156.615 | 39.3024  | 317.634 |
| F | 285        | F      | 54.1764  | 11.595   | 49.8732  | 114.7956 | 308.154  | 180.255 | 93.984   | 347.694 |
| G | 140        | G      | 292.8744 | 256.4814 | 139.932  | 108.8652 | 123.2616 | 169.026 | 34.176   | 470.94  |
| Н | 280        | Н      | 344.9052 | 339.9654 | 238.602  | 258.8196 | 443.4216 | 286.635 | 103.1688 | 374.748 |
|   |            | demand | 894      | 773      | 598      | 706      | 1334     | 985     | 356      | 1670    |

Table 1. Cost of delivery from warehouse to agency & Capacity of each warehouse

| i       | j        | k        | l        | m        | n        | 0        | р        | q        | r        | s       | t        | Capacity |
|---------|----------|----------|----------|----------|----------|----------|----------|----------|----------|---------|----------|----------|
| 28.812  | 56.1516  | 28.5768  | 42.4848  | 52.632   | 102.8016 | 203.3838 | 263.4    | 332.2752 | 397.9764 | 101.088 | 101.9472 | 7500     |
| 85.848  | 129.2256 | 50.5764  | 42.6852  | 94.248   | 139.0512 | 171.7902 | 279.204  | 255.9252 | 249.246  | 64.3968 | 87.3144  | 6000     |
| 120.54  | 172.6854 | 72.576   | 55.5108  | 119.952  | 163.4064 | 186.9288 | 298.1688 | 220.4988 | 164.2572 | 54.4752 | 80.7216  | 6500     |
| 189.924 | 295.7574 | 107.5032 | 73.7472  | 151.776  | 169.3536 | 178.3722 | 218.0952 | 14.0484  | 189.5904 | 74.5056 | 23.6376  | 8000     |
| 110.25  | 135.3792 | 44.4528  | 18.2364  | 82.2528  | 96.5712  | 12.5058  | 146.4504 | 164.3052 | 266.4072 | 86.8608 | 53.7072  | 6800     |
| 114.954 | 183.0696 | 105.0084 | 101.0016 | 137.088  | 202.7712 | 375.174  | 434.0832 | 437.3328 | 446.1912 | 90.2304 | 136.68   | 7200     |
| 162.582 | 220.3758 | 95.256   | 67.5348  | 144.9216 | 179.832  | 188.2452 | 285.5256 | 133.7652 | 26.1504  | 34.8192 | 59.8176  | 5500     |
| 104.958 | 105.3804 | 60.5556  | 58.5168  | 45.7776  | 7.9296   | 219.1806 | 128.5392 | 342.6588 | 529.5456 | 145.08  | 89.7264  | 4500     |
| 490     | 641      | 378      | 334      | 408      | 472      | 1097     | 878      | 1018     | 1362     | 312     | 268      |          |

\*. A~H: warehouse, a~t:agency

# 4. Genetic Algorithm Approach

In this paper, we propose a new coding method that is a matrix-form coding method. 2by2-method is very efficienty to control lethal gene in GA process.

## **Model Formulation**

We have the following variables: For each warehouse  $i \in m$  and agency  $j \in n$ ,  $d_{ij}$  is the cost from warehouse i to agency j. From each arc (i, j), the decision variable  $x_{ij}$  is equal to 1 if arc (i, j) is used (delivered) and 0 others, and variable  $y_j$  indicates that warehouse j will be held or not. Furthermore,  $f_j$  indicates a fixed cost of warehouse,  $w_i$  is demand of agency and  $C_j$  is capacity of warehouse. We minimize the total cost that consist of travel or time cost and a fixed cost. The object is, firstly minimize total cost and then decide decision variable  $y_j$ .

Min 
$$\sum_{i}^{m} \sum_{j}^{n} d_{ij} x_{ij} + \sum_{j}^{n} f_{j} y_{j}$$
s.t. 
$$\sum_{i} x_{ij} = 1$$

$$\sum_{i} w_{i} x_{ij} \leq C_{j} y_{j}$$

$$x_{ij} = \begin{cases} 1 : \text{ deliver warehouse } j \text{ agent } i \\ 0 : \text{ not deliver warehouse } j \end{cases}$$

$$y_{j} = \begin{cases} 1 : \text{ hold warehouse } j \\ 0 : \text{ not hold warehouse } j \end{cases}$$

## **Simulation**

Using genetic algorithms for SCN is similar to the TSP or Job Shop Scheduling Problem, as it often involves the use of order or position dependent genomes, since the optimum or best sequence of activities is sought. Hence, an illegal solution may have the same value multiple times in the genome ("superposition") and be missing other values. Technique that prevent creation of these 'lethal' individuals is important for the efficient execution of a GA, and is presented as a matrix-form coding method.

Table 2. Setting of GA-parameters

| GA-parameters             |                            |  |  |  |  |  |  |  |  |
|---------------------------|----------------------------|--|--|--|--|--|--|--|--|
| Crossover Probability     | 0.6                        |  |  |  |  |  |  |  |  |
| Mutation Probability      | 0.2                        |  |  |  |  |  |  |  |  |
| Selection Method          | Roulette wheel Strategy    |  |  |  |  |  |  |  |  |
| Population Size           | 20                         |  |  |  |  |  |  |  |  |
| Generations               | 5000                       |  |  |  |  |  |  |  |  |
| Random variable Algorithm | Mersenne Twister Algorithm |  |  |  |  |  |  |  |  |

We tested two methods; Genetic Algorithm, and Branch and Bound, so as to evaluate the performance using a data of Shapiro[9].

The best result from branch and bound method is Table 3. These table indicates that the warehouse A, C, E, G should be kept.

Table 3. Result of Branch and Bound Method

| Yj | Xij    | a   | b   | с   | d   | e    | f   | g   | h    | I   | j   | k   | 1   | m   | n   | О    | p   | q    | r    | s   | t   |
|----|--------|-----|-----|-----|-----|------|-----|-----|------|-----|-----|-----|-----|-----|-----|------|-----|------|------|-----|-----|
| 1  | A      | 1   | 1   | 0   | 0   | 0    | 0   | 0   | 1    | 1   | 1   | 1   | 0   | 1   | 0   | 0    | 0   | 0    | 0    | 0   | 0   |
| 0  | В      | 0   | 0   | 0   | 0   | 0    | 0   | 0   | 0    | 0   | 0   | 0   | 0   | 0   | 0   | 0    | 0   | 0    | 0    | 0   | 0   |
| 1  | С      | 0   | 0   | 1   | 1   | 1    | 1   | 1   | 0    | 0   | 0   | 0   | 0   | 0   | 0   | 0    | 0   | 0    | 0    | 0   | 0   |
| 0  | D      | 0   | 0   | 0   | 0   | 0    | 0   | 0   | 0    | 0   | 0   | 0   | 0   | 0   | 0   | 0    | 0   | 0    | 0    | 0   | 0   |
| 1  | Е      | 0   | 0   | 0   | 0   | 0    | 0   | 0   | 0    | 0   | 0   | 0   | 1   | 0   | 1   | 1    | 1   | 0    | 0    | 0   | 1   |
| 0  | F      | 0   | 0   | 0   | 0   | 0    | 0   | 0   | 0    | 0   | 0   | 0   | 0   | 0   | 0   | 0    | 0   | 0    | 0    | 0   | 0   |
| 1  | G      | 0   | 0   | 0   | 0   | 0    | 0   | 0   | 0    | 0   | 0   | 0   | 0   | 0   | 0   | 0    | 0   | 1    | 1    | 1   | 0   |
| 0  | Н      | 0   | 0   | 0   | 0   | 0    | 0   | 0   | 0    | 0   | 0   | 0   | 0   | 0   | 0   | 0    | 0   | 0    | 0    | 0   | 0   |
|    |        | 1   | 1   | 1   | 1   | 1    | 1   | 1   | 1    | 1   | 1   | 1   | 1   | 1   | 1   | 1    | 1   | 1    | 1    | 1   | 1   |
|    |        | 1   | 1   | 1   | 1   | 1    | 1   | 1   | 1    | 1   | 1   | 1   | 1   | 1   | 1   | 1    | 1   | 1    | 1    | 1   | 1   |
|    | Demand | 894 | 773 | 598 | 706 | 1334 | 985 | 356 | 1670 | 490 | 641 | 378 | 334 | 408 | 472 | 1097 | 878 | 1018 | 1362 | 312 | 268 |

Objective function 1843.2672

|          |        | Capac | ity  |
|----------|--------|-------|------|
| Restrict | 5254 < | 7500  | 7500 |
|          | 0 <    | 6000  | 0    |
|          | 3979 < | 6500  | 6500 |
|          | 0 <    | 8000  | 0    |
|          | 3049 < | 6800  | 6800 |
|          | 0 <    | 7200  | 0    |
|          | 2692 < | 5500  | 5500 |
|          | 0 <    | 4500  | 0    |

The result from GA is below Table 4. This solution has a matrix-form because of the chromosome is coded as matrix-form. By this coding method, we can control lethal genes conveniently.

Table 4. Result of GA

| 1 1 0 0 0 0 0 1 1 1 1 0 1 0 0 0 0 0 0 0                      | → 1             |
|--|-----------------|
| $0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \$                    | $\rightarrow 0$ |
| $0\ 0\ 1\ 1\ 1\ 1\ 1\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0$    | $\rightarrow$ 1 |
| $0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \$                    | $\rightarrow 0$ |
| $0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 1\ 0\ 1\ 1\ 1\ 1\ 0\ 0\ 0\ 1$ | $\rightarrow 1$ |
| $0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \$                    | $\rightarrow 0$ |
| $0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \$                    | $\rightarrow 1$ |
| $0 \; 0 \; 0 \; 0 \; 0 \; 0 \; 0 \; 0 \; 0 \; 0 \;$          | $\rightarrow 0$ |
|  |                 |

Minimum Cost :1843.27 Generation :1072

GAs contain operators called crossover and mutation, the ones that specially affect performance of GA. Therefore, it is very important to specify the GA's parameter for getting a good performance. However it is very troublesome to identify GA-parameters. In the present paper, we use Experimental Design Method to set up GA parameters proposed by HAN [5] and then set up as Table 2. Validation of an analytical method through a series of experiments demonstrates that the method is suitable for its intended purpose. By Experimental Design method, we can expect to get a better result and to reduce the cost.

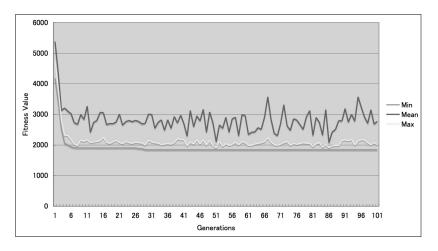


Figure 2. The value of fitness per each generations

# 5. Concluding remarks

Even if the result of alternatives do not seem to provide enough insight on decision making, by carrying out a genetic algorithm method, we can derive the overall solution by making the best use of them. In general, the relative importance of criteria is ambiguous and the scores are imprecise. It suggests that, in such cases, a genetic algorithm method is useful. Moreover, we modified coding

method of chromosome to adapt them appropriately to SCN with controlling lethal gene.

Furthermore, we compared GA and Branch and Bound method to identify the validity of GA. Our proposed algorithm more computational time than others, but it is trifling difference, because our focus is not the speed of algorithm but the accuracy of the result. GA is valid not only a realistic problem but also the homogeneous combinatorial optimization problem.

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